

# Inspire Create Transform

# Medellín Air qUality Initiative



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# Outline

Introduction

Why MAul

Model Predictive Control

Measurement

Models

Uncertainty reduction

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Conclusions



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# Introduction



Marzo 6 2018 9:52 am

Marzo 11 2018 9:53 am

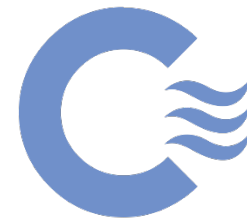


# Why MAul?

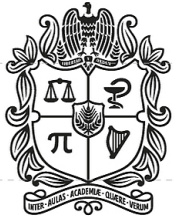


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## WORKSHOP Atmospheric Pollution and its Impacts



SESQUICENTENARIO



UNIVERSIDAD NACIONAL DE COLOMBIA



Desert Research Institute



UNIVERSIDAD DE ANTIOQUIA



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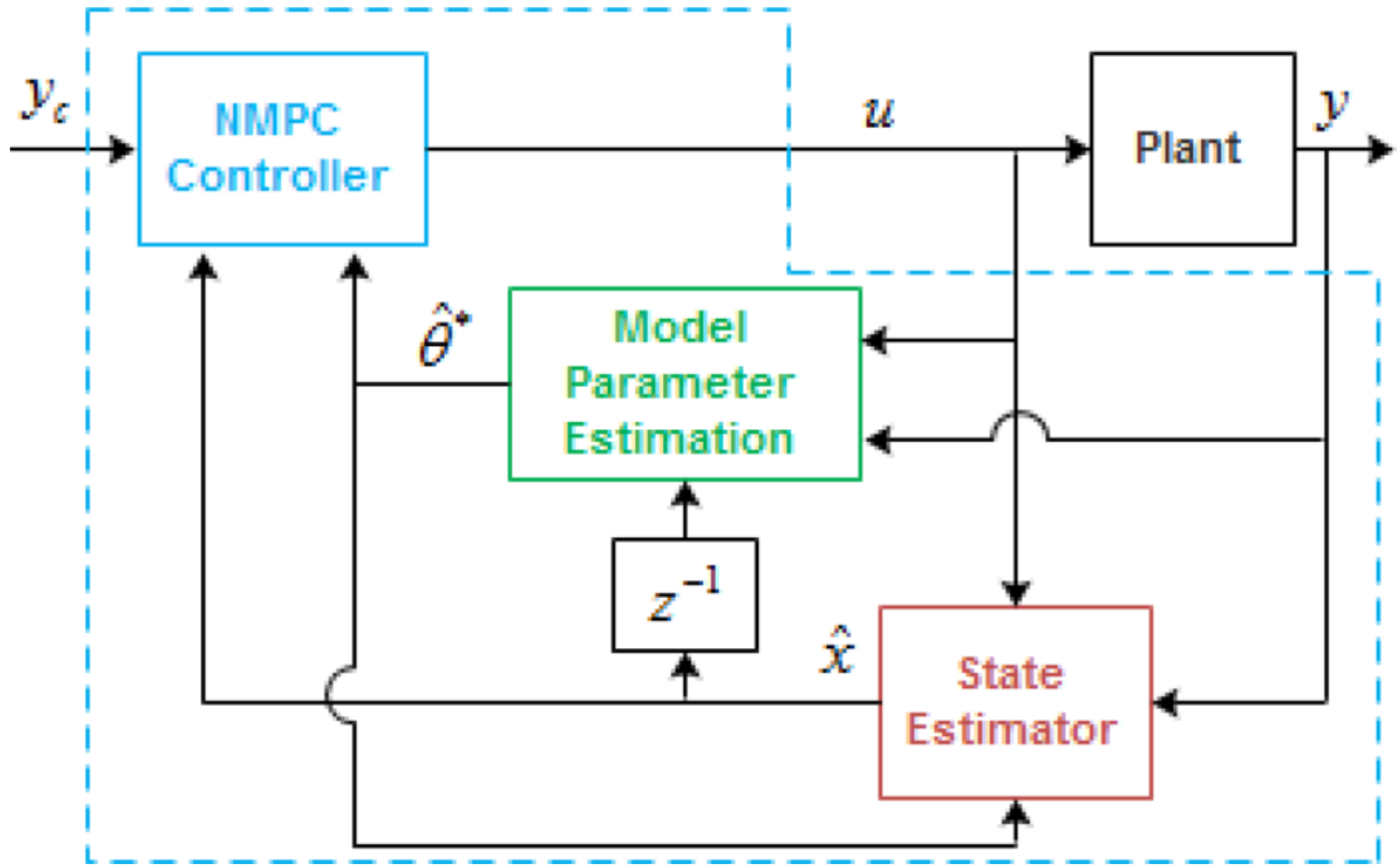
TNO innovation for life

Inspire Create Transform

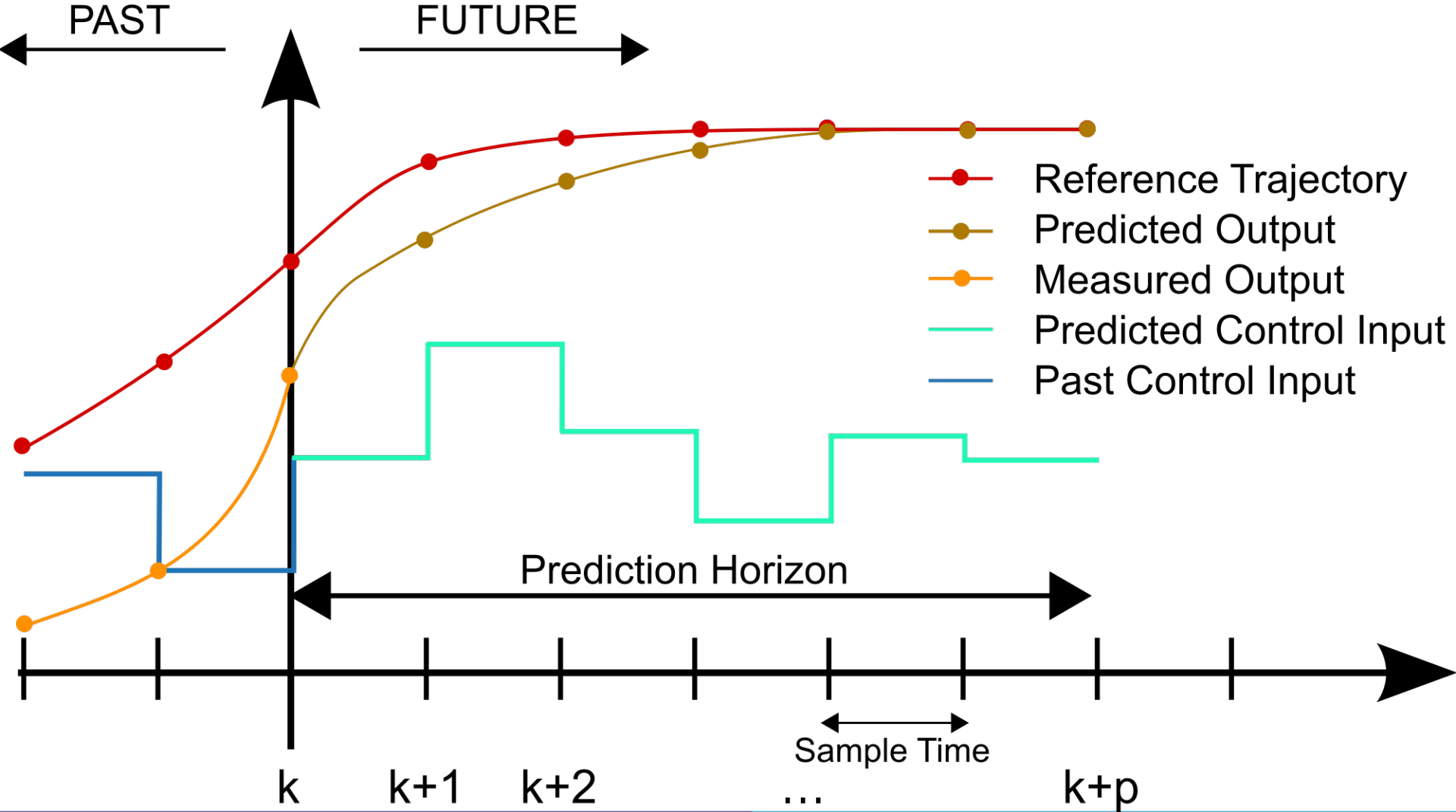
Vigilada Mineducación

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# Model Predictive Control

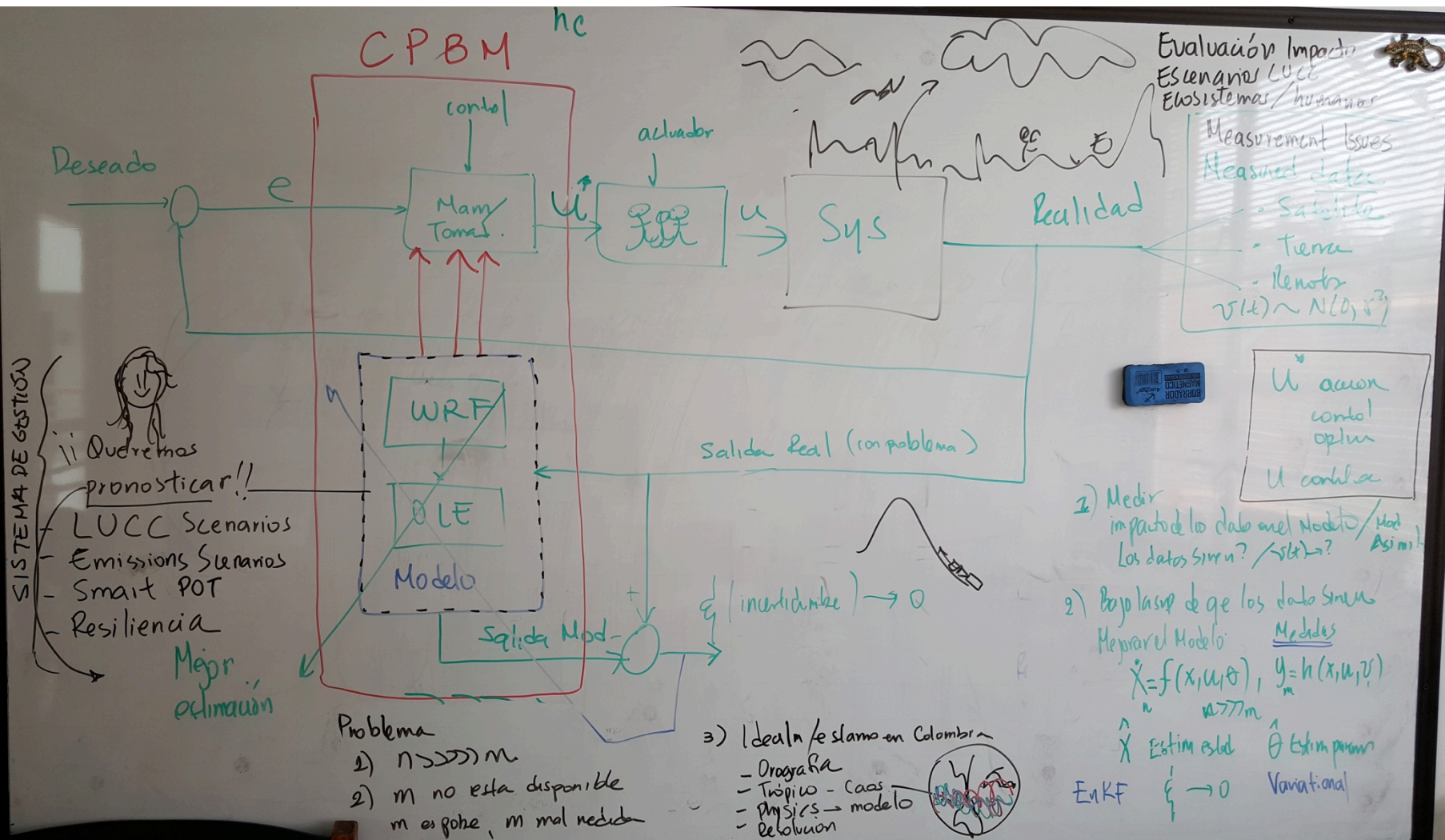


# Model Predictive Control

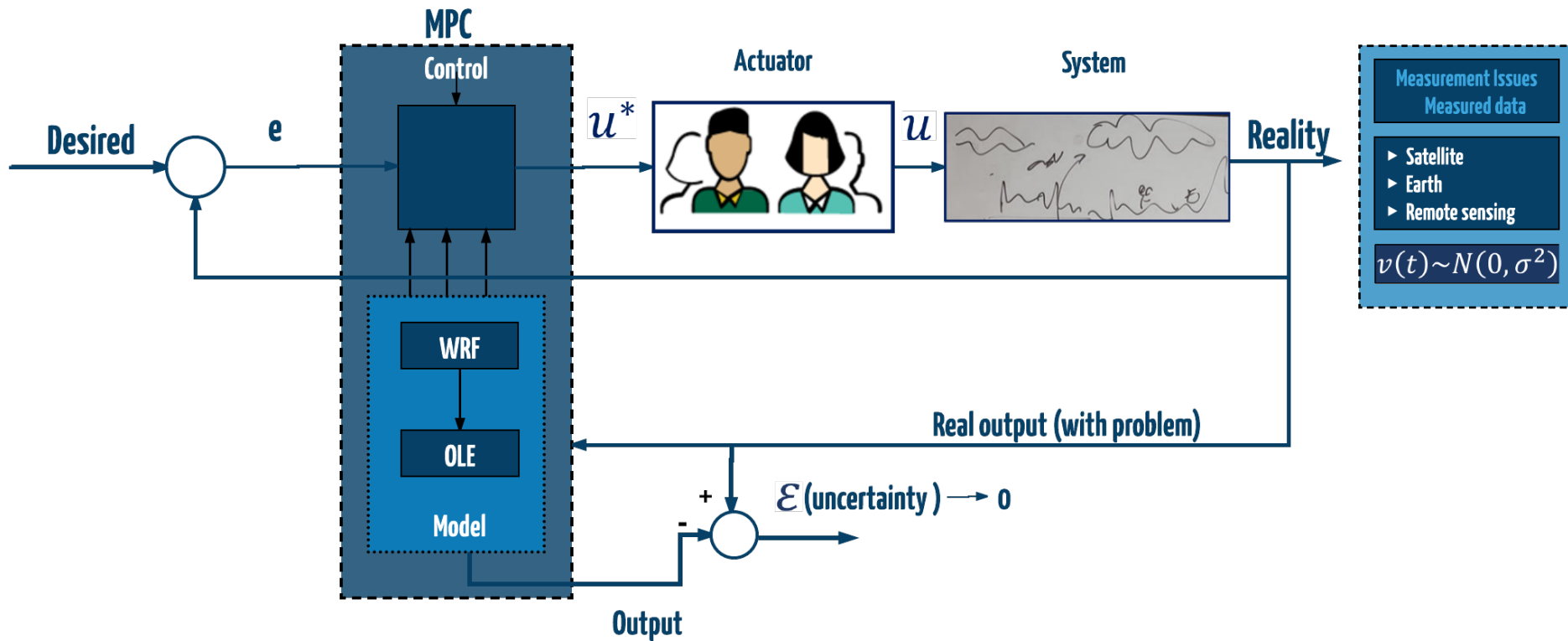




# Model Based Predictive Control Scheme

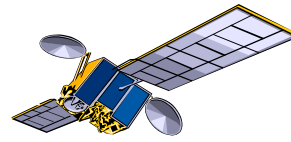
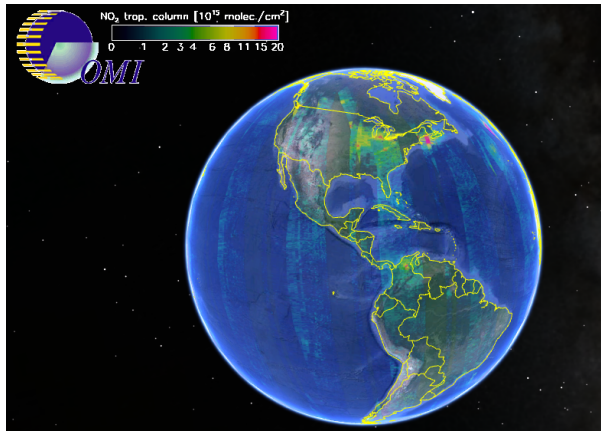


# Model Based Predictive Control Scheme





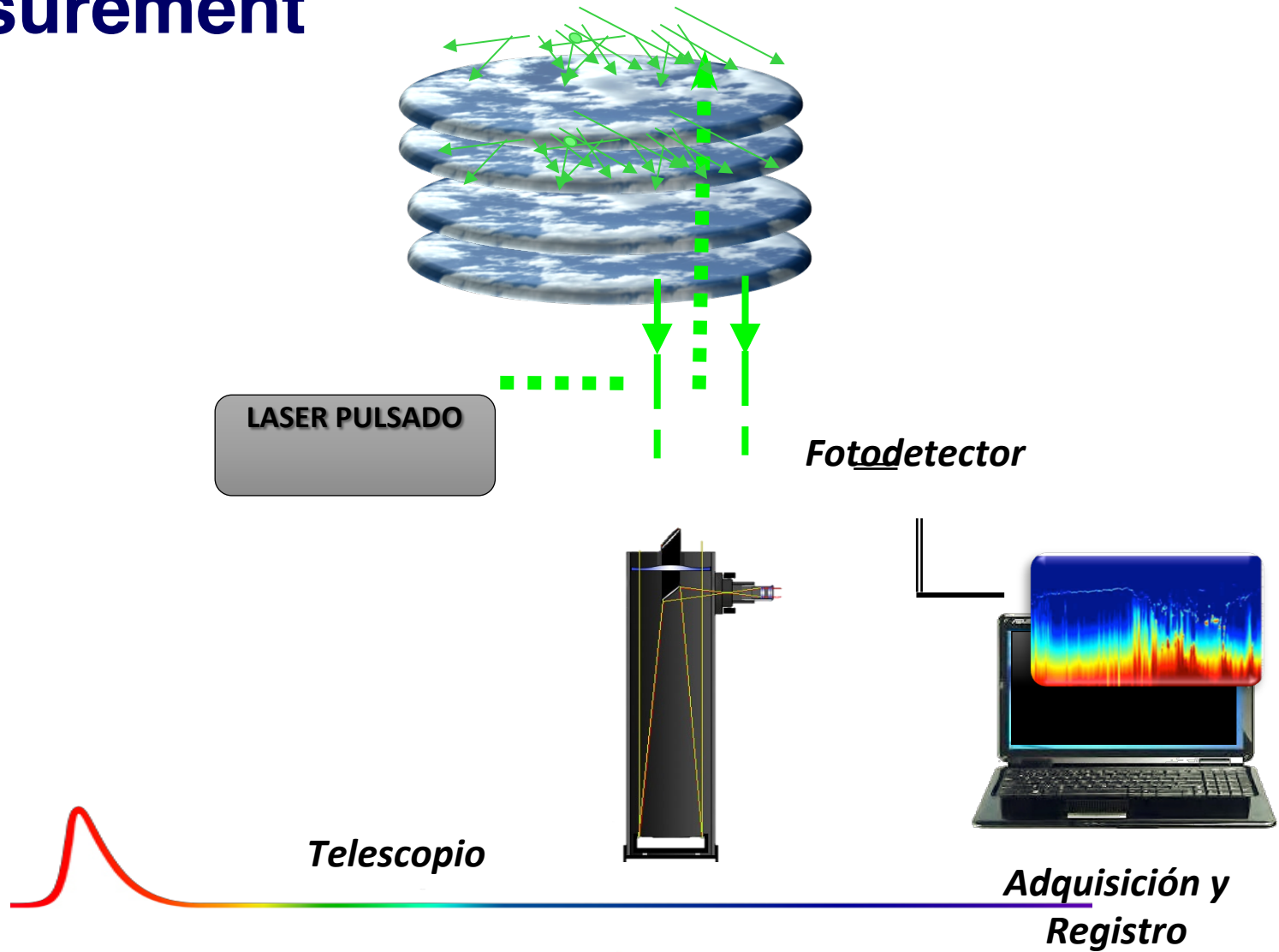
# Measurement



Biomonitor  
(*Tillandsia r.*)



# Measurement



# Models

Chemistry transport Model  
LOTOS- EUROS

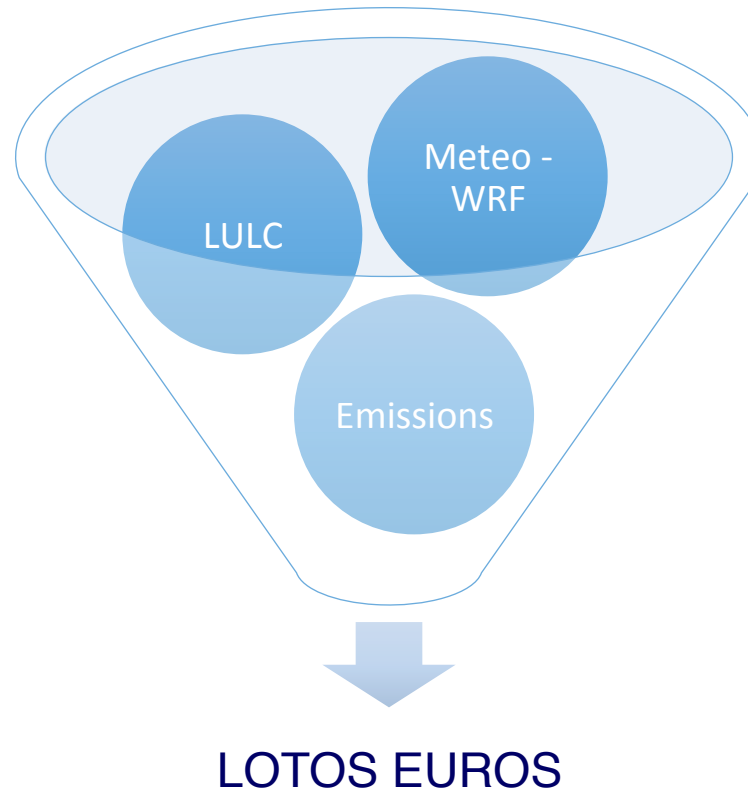
$$\frac{\partial C}{\partial t} + U \frac{\partial C}{\partial x} + V \frac{\partial C}{\partial y} + W \frac{\partial C}{\partial z} = \frac{\partial}{\partial t} \left( K_h \frac{\partial C}{\partial x} \right) + \frac{\partial}{\partial y} \left( K_h \frac{\partial C}{\partial y} \right) + \frac{\partial}{\partial z} \left( K_z \frac{\partial C}{\partial z} \right)$$

$$+ E + R + Q - D - W$$

**TNO** innovation  
for life

# Models

Chemistry transport Model  
LOTOS- EUROS



# Models

Weather research Forecast WRF

$$\partial_t U + m_x [\partial_x(Uu) + \partial_y(Vu)] + \partial_\eta(\Omega u)$$

$$+ (m_x/m_y)(\alpha/\alpha_d) [\mu_d(\partial_x\phi' + \alpha_d\partial_x p' + \alpha'_d\partial_x\bar{p}) + \partial_x\phi(\partial_\eta p' - \mu'_d)] = F_U$$

$$\partial_t V + m_y [\partial_x(Uv) + \partial_y(Vv)] + (m_y/m_x)\partial_\eta(\Omega v)$$

$$+ (m_x/m_y)(\alpha/\alpha_d) [\mu_d(\partial_x\phi' + \alpha_d\partial_x p' + \alpha'_d\partial_x\bar{p}) + \partial_x\phi(\partial_\eta p' - \mu'_d)] = F_U$$

$$\partial_t W + (m_x m_y/m_y) [\partial_x(Uw) + \partial_y(Vw)] + \partial_\eta(\Omega w)$$

$$- m_y^{-1} g(\alpha/\alpha_d) [\partial_\eta p' - \bar{\mu}_d(q_v + q_c + q_r)] + m_y^{-1} \mu'_d g = F_W,$$

$$\partial_t \mu'_d + m_x m_y [\partial_x U + \partial_y V] + m_y \partial_\eta \Omega = 0$$

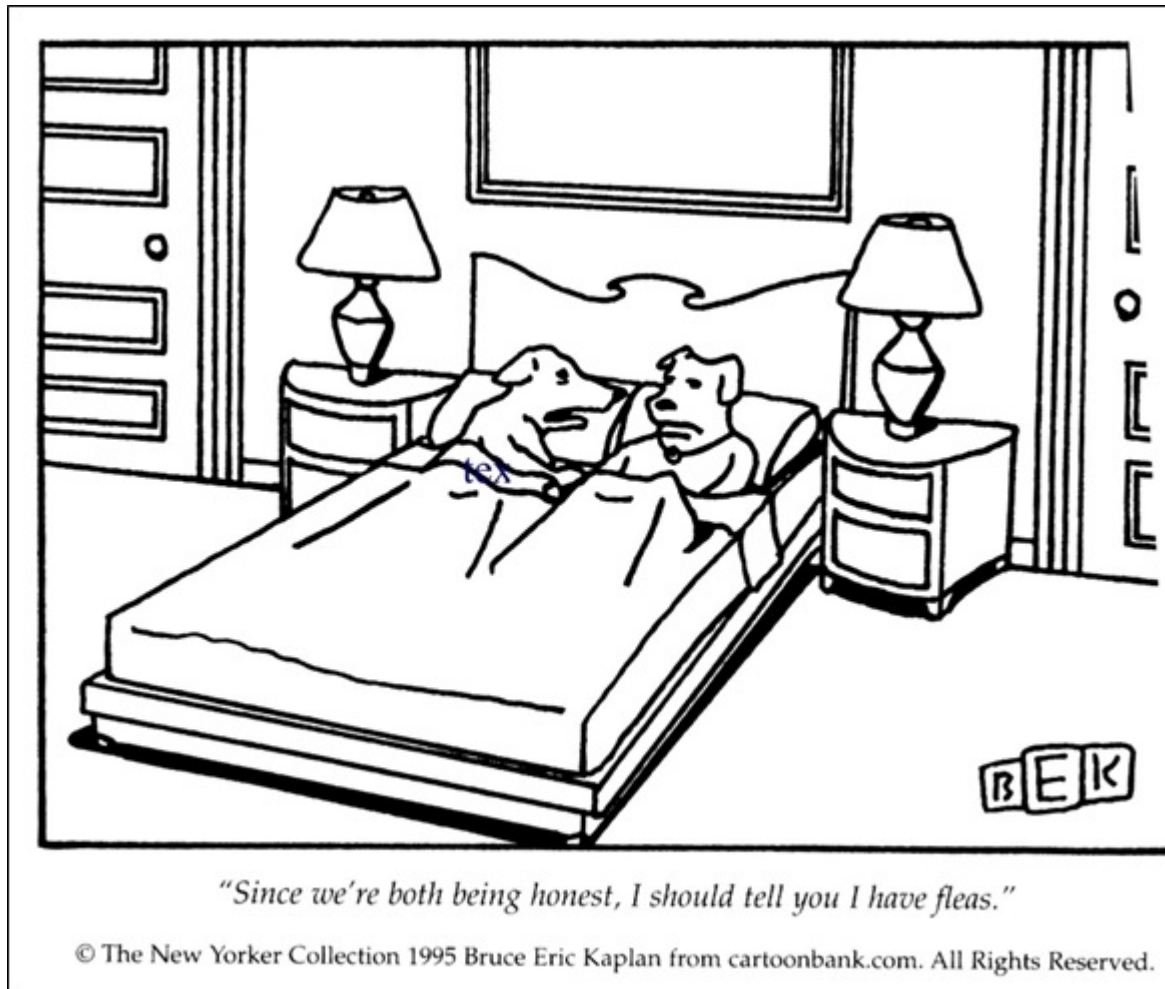
$$\partial_t \phi' + \mu_d^{-1} [m_x m_y (U \partial_x \phi + V \partial_y \phi) + m_y \Omega \partial_\eta \phi - m_y g W] = 0.$$

$$\partial_t \Theta + m_x m_y [\partial_x(U\theta) + \partial_y(V\theta)] + m_y \partial_\eta(\Omega\theta) = F_\Theta$$

$$\partial_t Q_m + m_x m_y [\partial_x(Uq_m) + \partial_y(Vq_m)] + m_y \partial_\eta(\Omega q_m) = F_{Q_m}.$$

$$\partial_\eta \phi' = -\bar{\mu}_d \alpha'_d - \alpha_d \mu'_d.$$

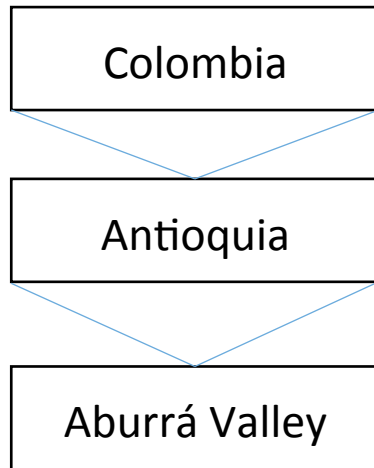
# Uncertainty Reduction



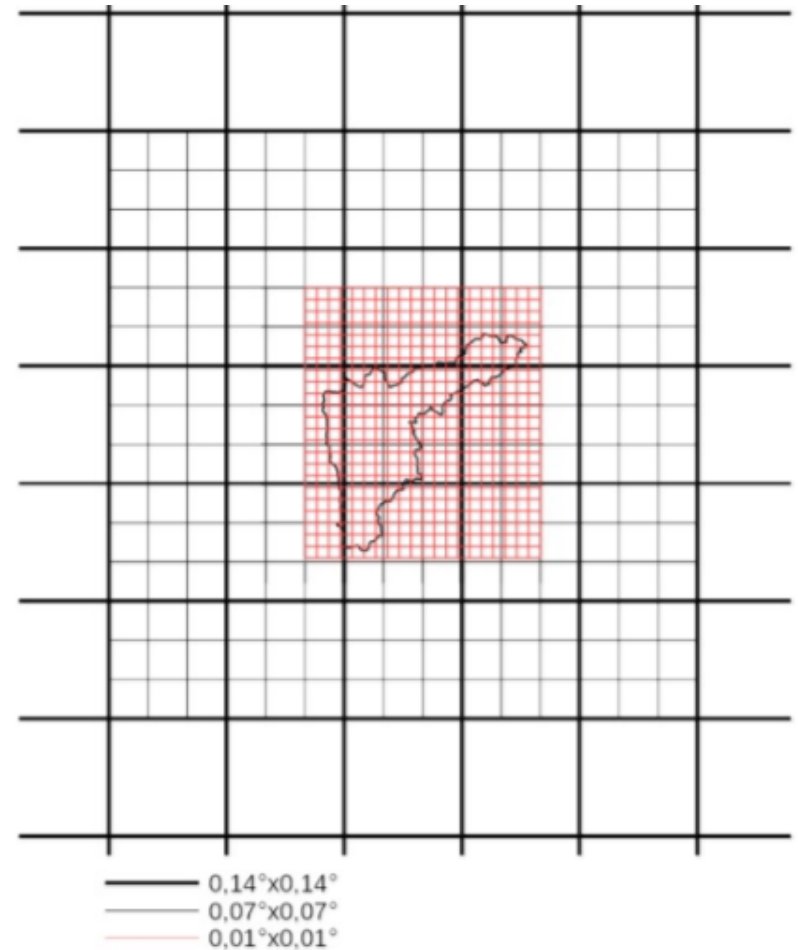


# Modeling and Simulation

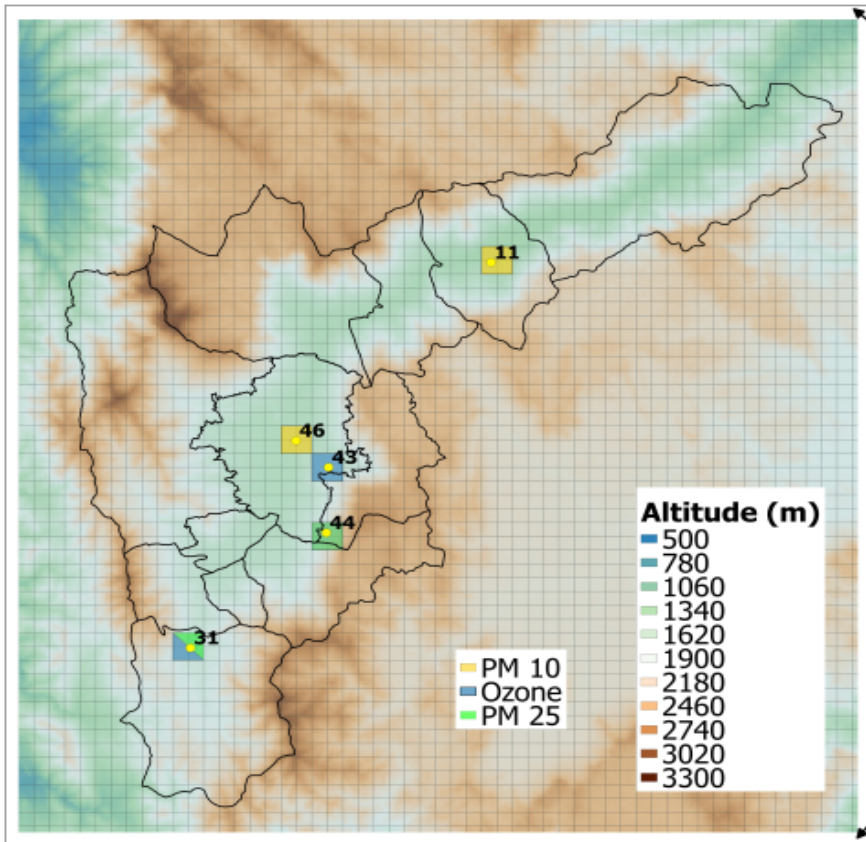
Nested domains



0.7 Degrees 77.86 Km Long x 77,71 Km Lat  
0.14 Degrees 15.6 Km Long x 15,4 Km Lat  
0.07 Degrees 7.8 Km Long x 7,7 Km Lat  
0.01 Degrees 1.11 Km Long x 1,1 Km Lat

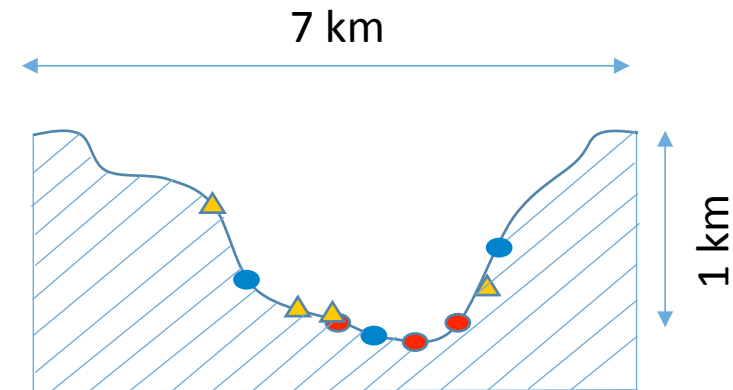


# Model assimilation for Medellin



Topographical map of the region under study, showing the political boundaries of the Aburrá Valley cities.

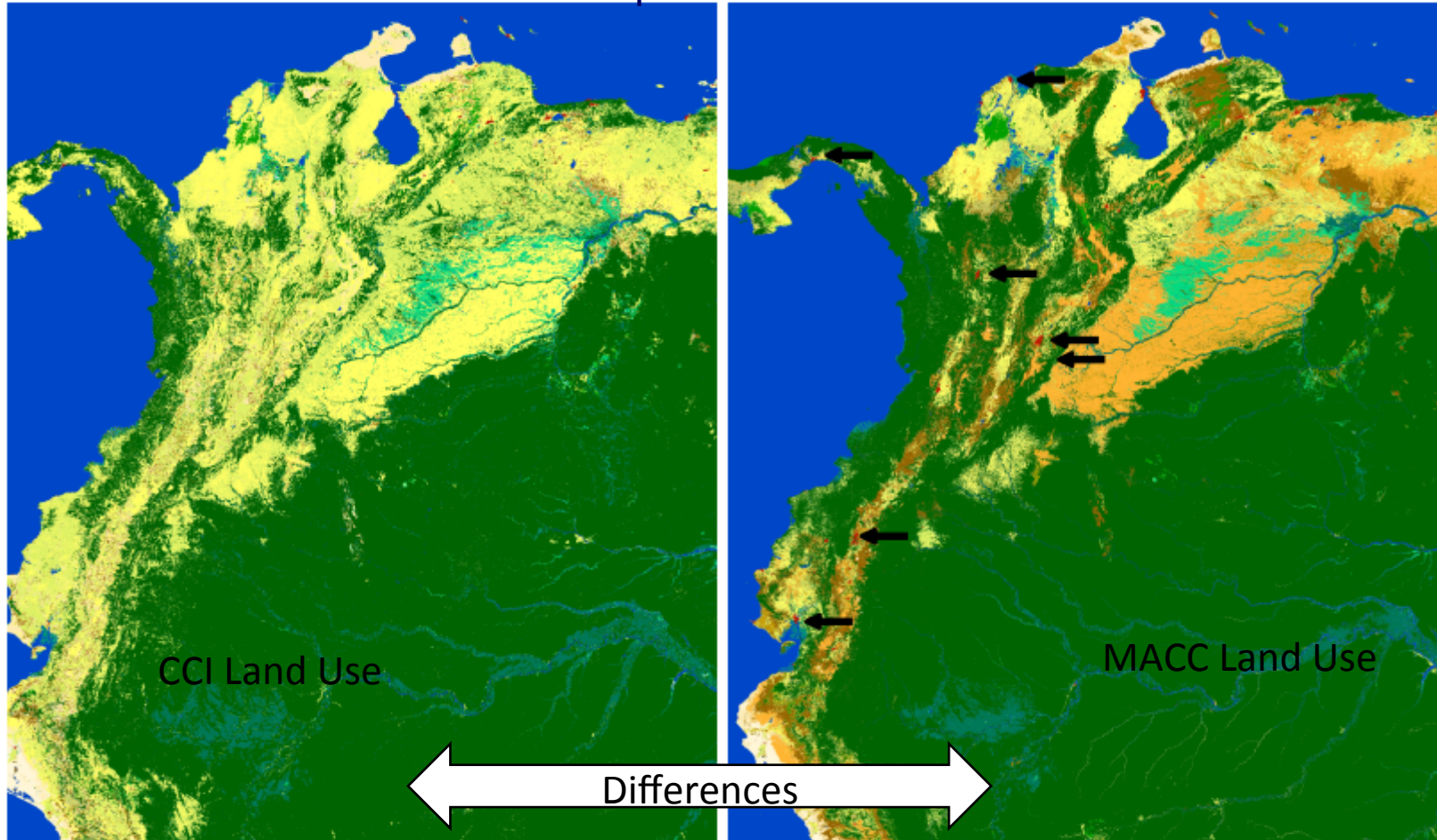
Topographical characteristic of Aburrá deep-seated mountain valley



- ▲ Citizens
- Ground based measurements
- Roads

# Sources of uncertainty of L.E in Colombia

Inputs Land Use/ Land Cover to be updated



Data assimilation relies on the use of an extension for high dimensional systems of the classical approach for filtering called the Kalman Filter

$$\mathbf{x}_k = \mathcal{M}_{k,k-1}(\mathbf{x}_{k-1}) + \mathbf{u}_k,$$

$$\mathbf{y}_k = \mathcal{H}_k(\mathbf{x}_k) + \mathbf{v}_k.$$

$$\mathbf{x}_k \in \mathbb{R}^{m_x} \quad \mathbf{y}_k \in \mathbb{R}^{m_y} \quad \mathbf{u}_k \in \mathbb{R}^{m_x} \quad \mathbf{v}_k \in \mathbb{R}^{m_y}$$

$$\mathcal{M}_{k,k-1}: \mathbb{R}^{m_x} \rightarrow \mathbb{R}^{m_x} \quad \mathcal{H}_k: \mathbb{R}^{m_x} \rightarrow \mathbb{R}^{m_y}$$

[Evensen, 2009]  $\mathbf{u}_k$  and  $\mathbf{v}_k$  are independent white noise

The EnKF is a modification that uses Monte Carlo approach to estimate the minimum variance solution to the state estimation problem.

At the analysis step in the EnKF, an ensemble of the system state, is generated with sample mean and covariance as the analysis state and error covariance matrix with the ensemble  $n$  typically much smaller than the dimension  $m \times n$  in large scale applications.

$$\mathbf{X}_{k-1}^a = \{\mathbf{x}_{k-1,i}^a : i = 1, 2, \dots, n\}$$

By propagating the analysis ensemble through the transition operator, we obtain forecast ensemble at the next data assimilation cycle.

$$\mathbf{X}_k^f = \{\mathbf{x}_{k,i}^f : \mathbf{x}_{k,i}^f = \mathcal{M}_{k-1,k}(\mathbf{x}_{k-1,i}^a) + \mathbf{u}_{k,i}, i = 1, 2, \dots, n\}$$

When a new observation is available, the analysis step is used to compute the analysis ensemble from its forecast counterpart based on the sample covariance matrix of the forecast ensemble.



Two types of data assimilation:

- Related to the Ensemble Kalman filter for state estimation

$$\mathbf{x}_{k,i}^a = \mathbf{x}_{k,i}^f + \mathbf{K}_k [\mathbf{y}_{k,i}^s - \mathcal{H}_k(\mathbf{x}_{k,i}^f)], \quad \text{for } i = 1, 2, \dots, n,$$

$$\mathbf{K}_k = \hat{\mathbf{P}}_k^{xy} (\hat{\mathbf{P}}_k^{yy} + \mathbf{R}_k)^{-1},$$

$$\hat{\mathbf{S}}_k^f = \frac{1}{\sqrt{n-1}} [\mathbf{x}_{k,1}^f - \hat{\mathbf{x}}_k^f, \dots, \mathbf{x}_{k,n}^f - \hat{\mathbf{x}}_k^f],$$

$$\hat{\mathbf{S}}_k^{yy} = \frac{1}{\sqrt{n-1}} [\mathbf{y}_{k,1}^f - \hat{\mathbf{y}}_k^f, \dots, \mathbf{y}_{k,n}^f - \hat{\mathbf{y}}_k^f],$$

$$\mathbf{x}_{k,i}^a = \hat{\mathbf{x}}_k^a + \sqrt{n} (\mathbf{L}_k \mathbf{C}_k \mathbf{\Xi}_k)_i, \quad \text{for } i = 1, \dots, n$$

$$(\delta \mathbf{x}_{k,i})_j = (\hat{p}_{xy,k}^j / \hat{p}_{yy,k}^f) \delta y_{k,i}, \quad j = 1, \dots, m_x,$$

- Variational methods for the parameter estimation

$$X(t_{i+1}) = M_i X(t_i), \quad i = 1, \dots, m-1, \quad X(t_{i+1}) \in \mathfrak{R}^n$$

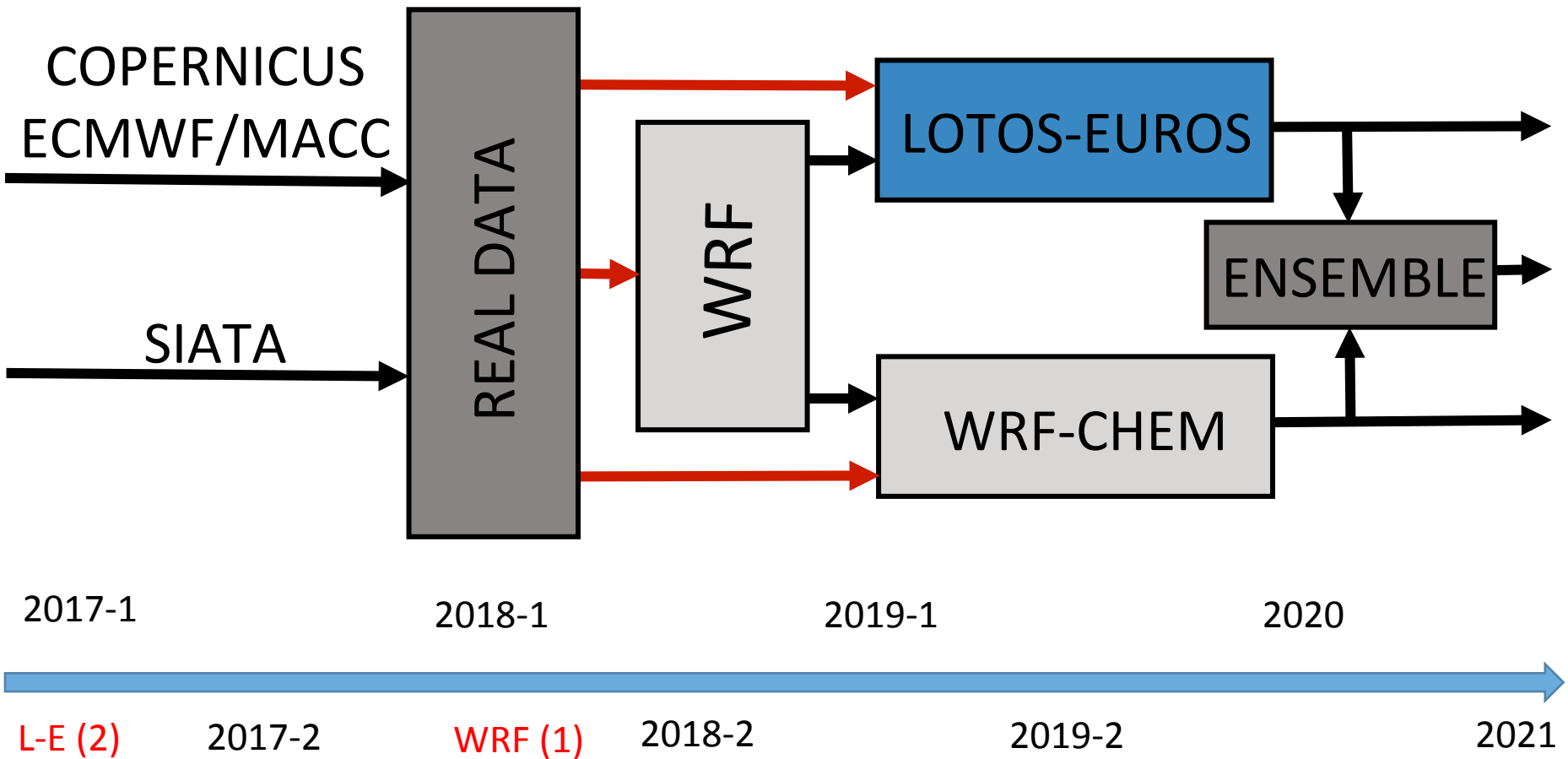
$$Y(t_i) = H(X(t_i)) + \eta(t_i), \quad H : \mathfrak{R}^n \rightarrow \mathfrak{R}^q$$

$$J(X_0) = \frac{1}{2} (X^b - X_0)^T B_0^{-1} (X^b - X_0) + \frac{1}{2} \sum_i (Y(t_i) - H(X(t_i)))^T R_i^{-1} (Y(t_i) - H(X(t_i))),$$

[Barbu 2010, Krymskaya, 2013, Sebacher, 2014, Altaf 2015, Fu et al, 2015, Lu et al, 2015, Krymskaya, 2013, Tijana et al, 2014 Verlaan and Sumihar, 2016 ]

# Ensemble-Based twin experiments

Localization and impact quantification strategies



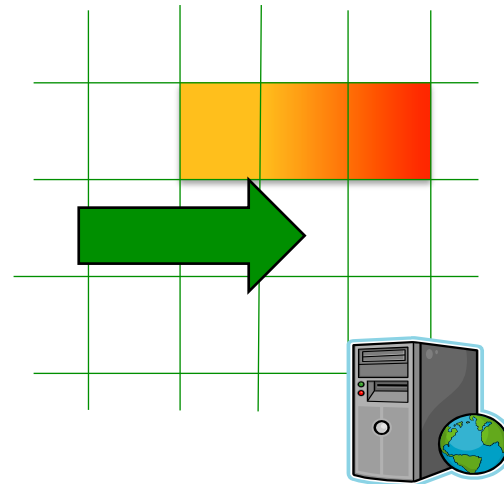
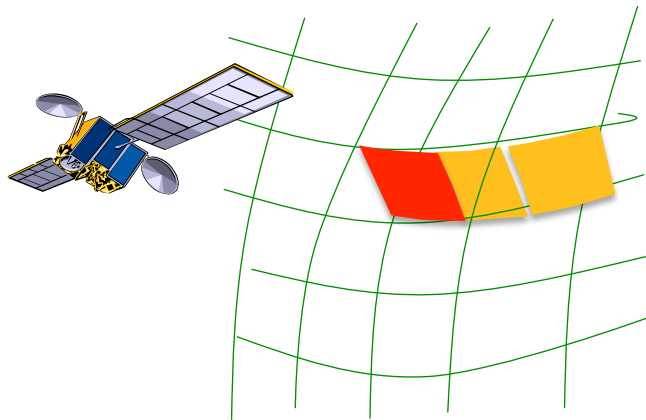
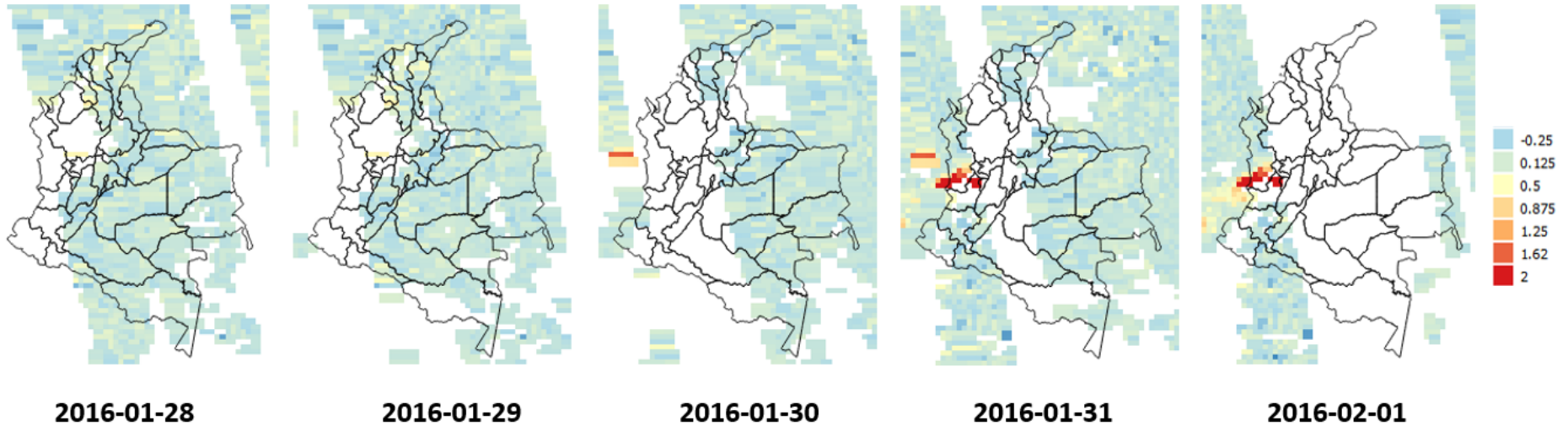
# Challenges



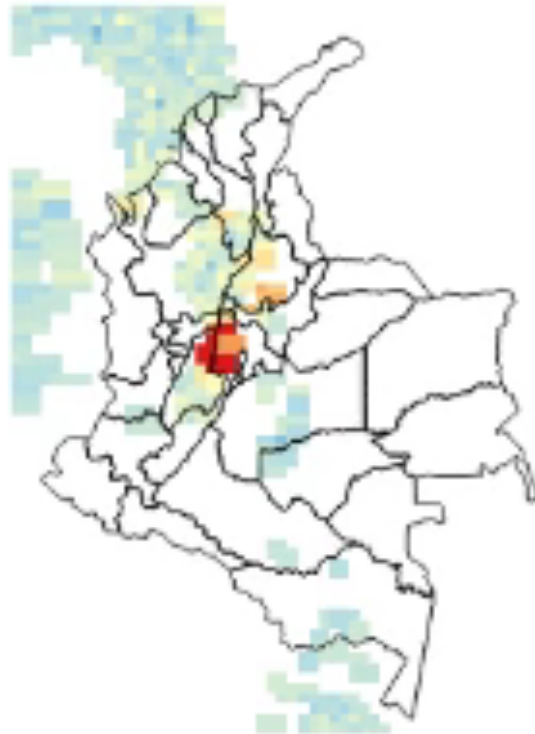
Spatial resolution: ~ 25 km x 25 km

Temporal resolution: 1 image per day of the same point,  
sun-synchronous orbit, 1:40 pm nadir capture over Colombia

# Challenges



# Challenges

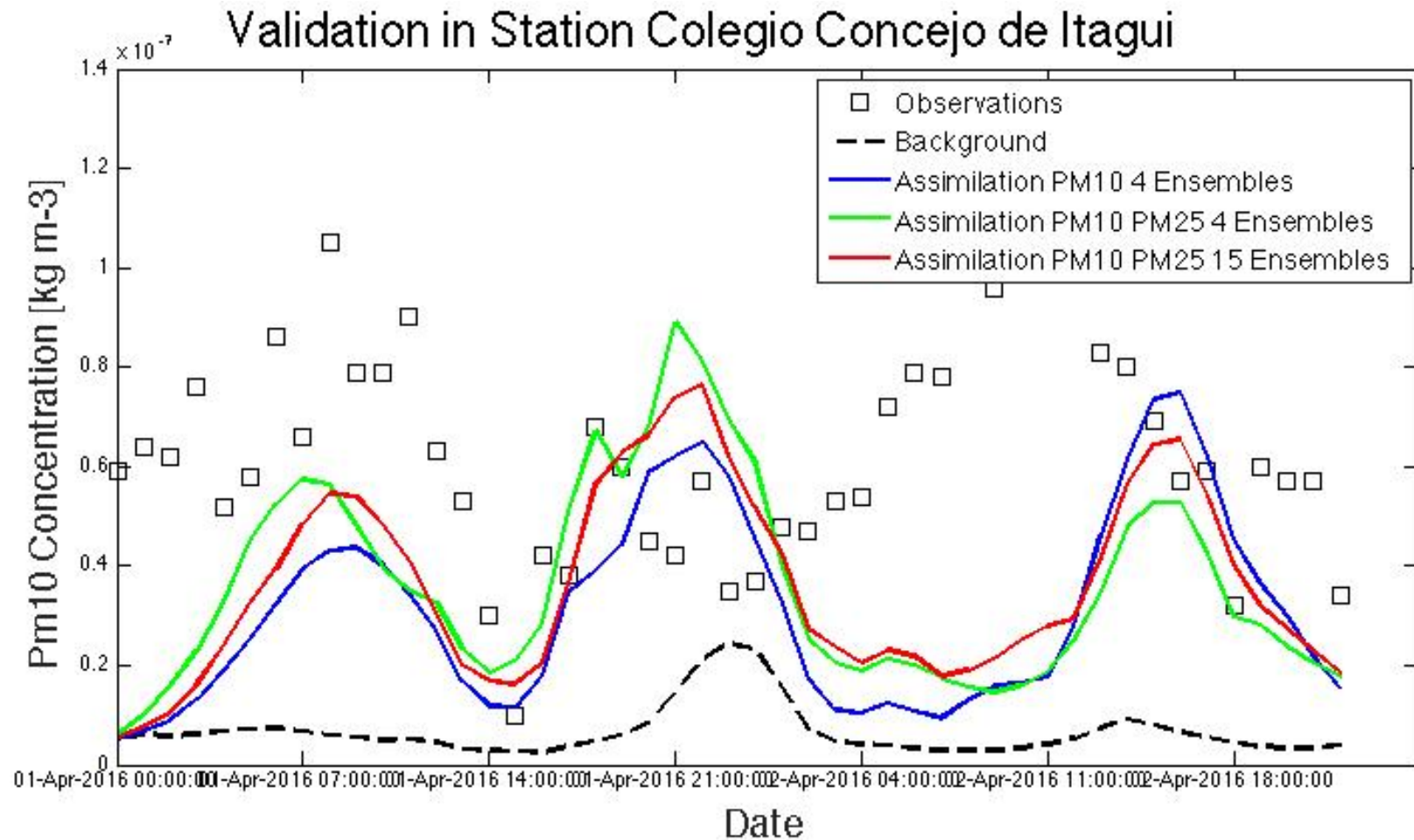


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SO2 OMI data example

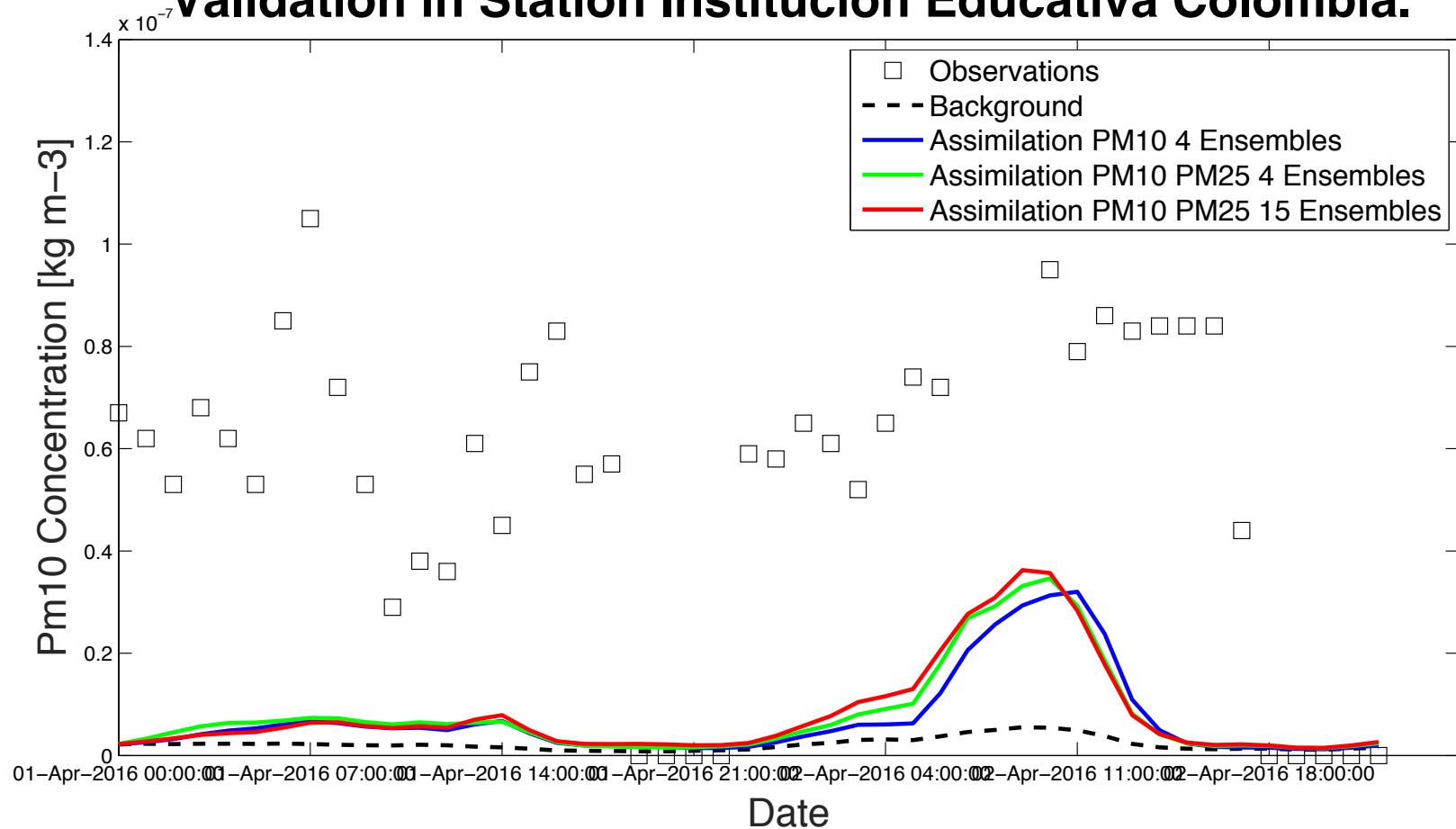


# Conclusions



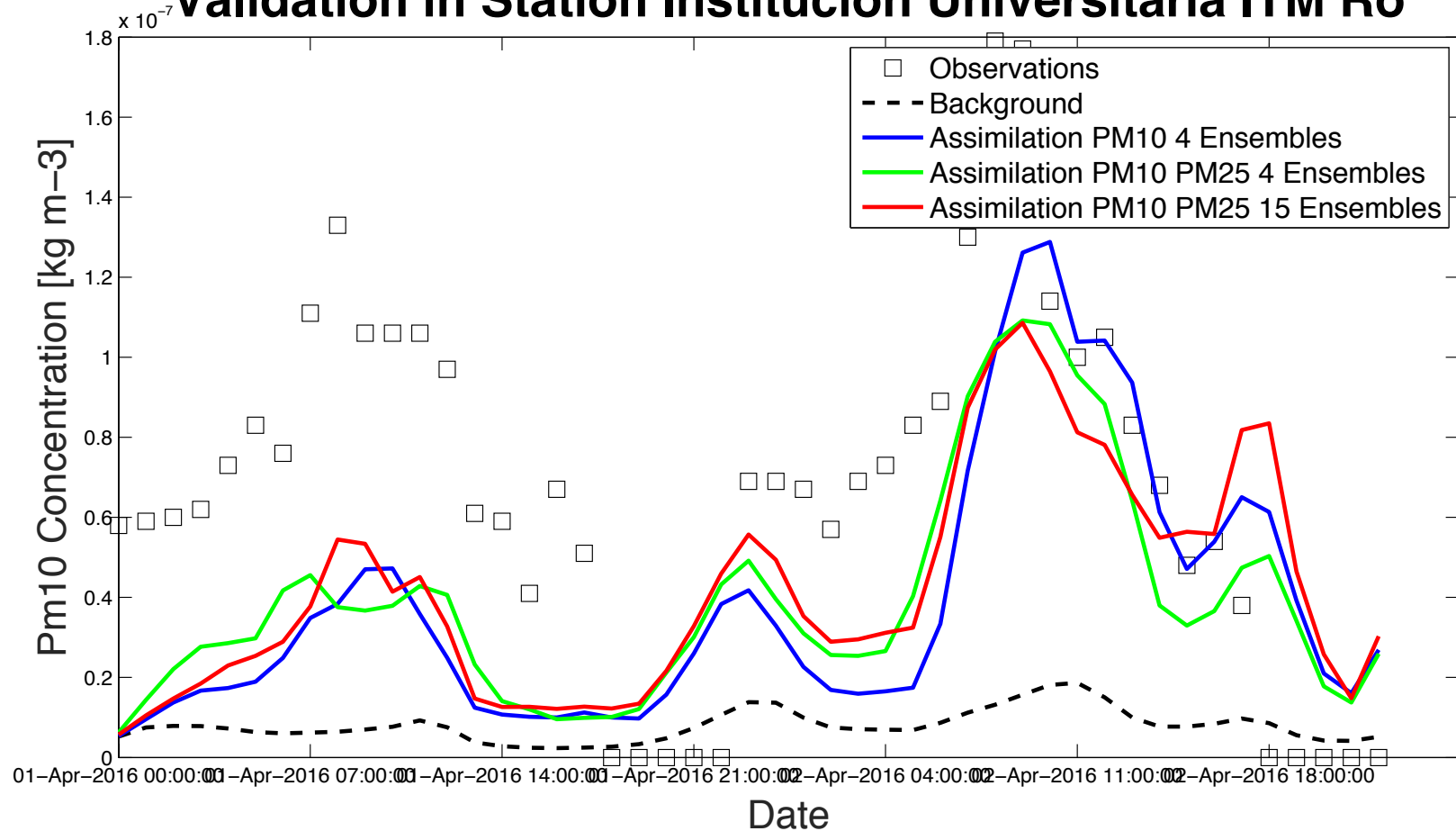
# Conclusions

## Validation in Station Institución Educativa Colombia.



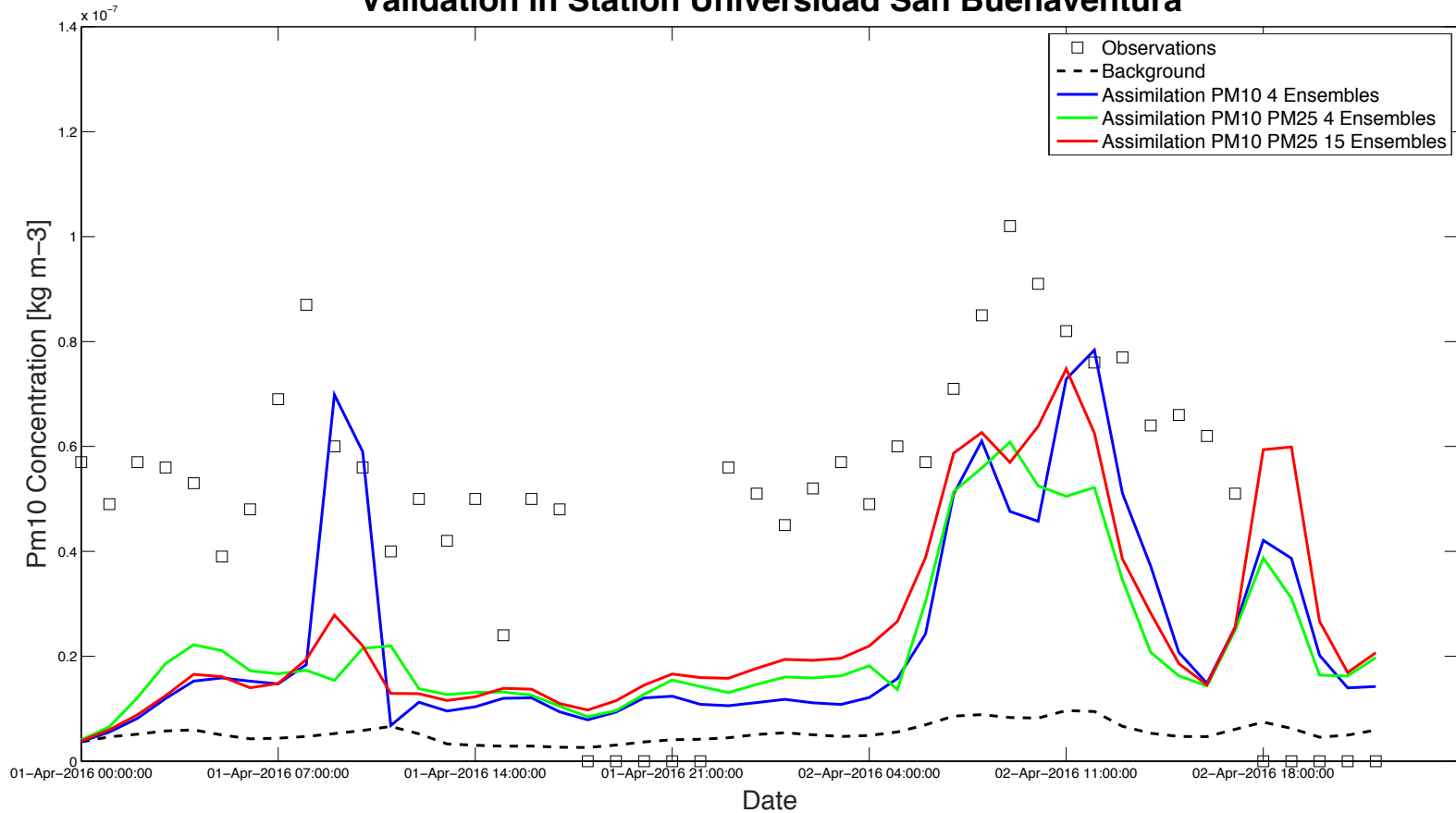
# Conclusions

## Validation in Station Institución Universitaria ITM Ro



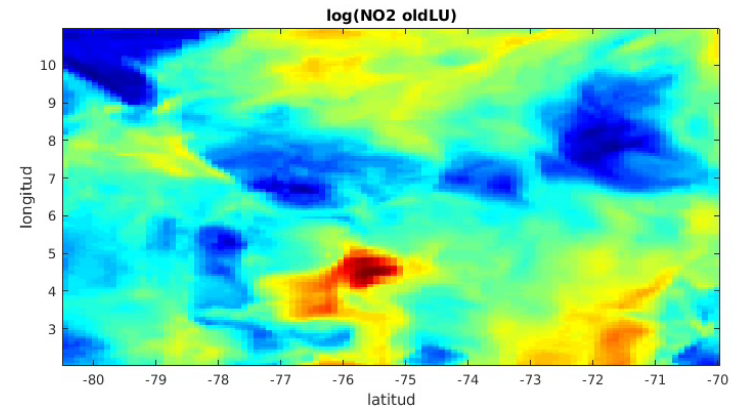
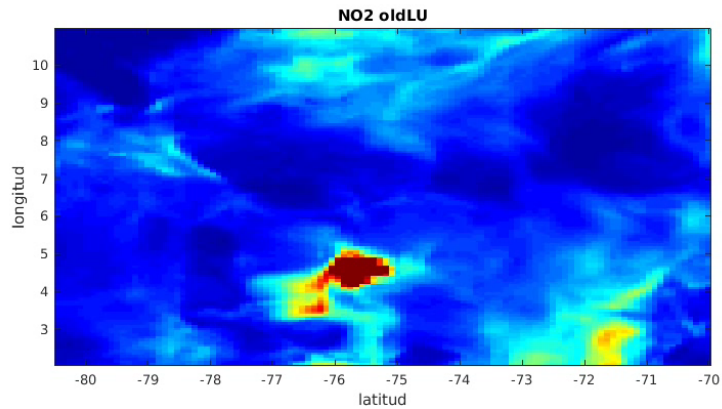
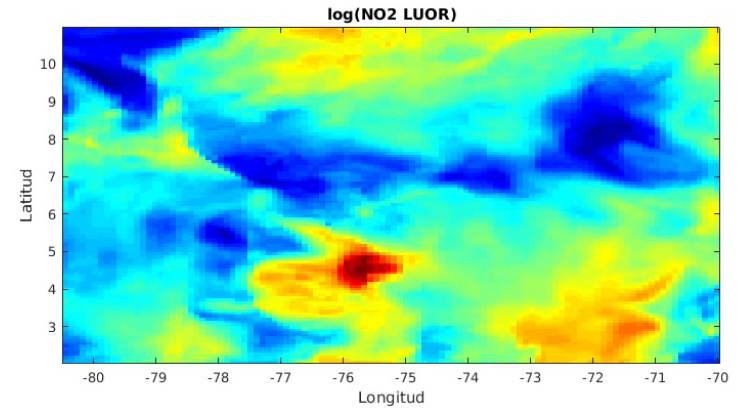
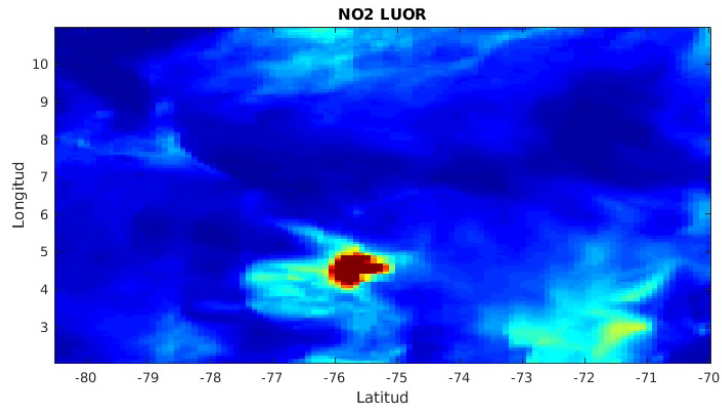
# Conclusions

## Validation in Station Universidad San Buenaventura



# Conclusions

Figure 1



# Conclusions

LOTOS-EUROS Coupling with a meteorological model like WRF. The WRF model is currently implemented in the region for the GIGA Research Group of the Universidad de Antioquia.

WRF is able to do a representation of the meteorology in a higher resolution than the databases available for the region.

Data Assimilation and integration with Traffic models



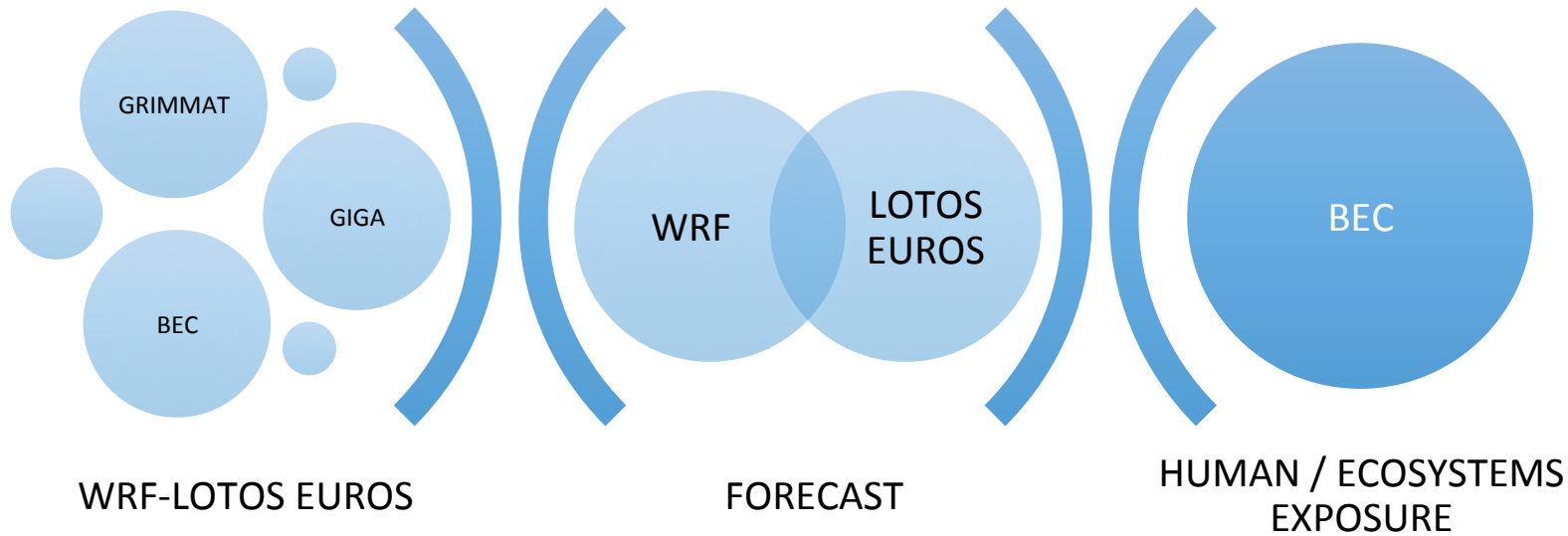
European Research Council  
Established by the European Commission

## ***Scale-FreeBack***

Advanced Grant 2015

**Scale-Free Control for Complex  
Physical Network Systems**





# Thanks



# Thanks

CENTRO DE COMPUTACIÓN CIENTÍFICA APOLO – Pineda,  
Mateo y Andrés!

DIRECCIÓN DE INFORMÁTICA – Delio y Hugo!

# Thank you all!

